

### 1. Problem

For 56 firms the number of employees  $X$  and the amount of expenses for continuing education  $Y$  (in EUR) were recorded. The statistical summary of the data set is given by:

|          | Variable $X$ | Variable $Y$ |
|----------|--------------|--------------|
| Mean     | 46           | 220          |
| Variance | 140          | 1827         |

The correlation between  $X$  and  $Y$  is equal to 0.61.

Estimate the expected amount of money spent for continuing education by a firm with 44 employees using least squares regression.

### Solution

First, the regression line  $y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$  is determined. The regression coefficients are given by:

$$\hat{\beta}_1 = r \cdot \frac{s_y}{s_x} = 0.61 \cdot \sqrt{\frac{1827}{140}} = 2.20361,$$
$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \cdot \bar{x} = 220 - 2.20361 \cdot 46 = 118.63386.$$

The estimated amount of money spent by a firm with 44 employees is then given by:

$$\hat{y} = 118.63386 + 2.20361 \cdot 44 = 215.593.$$