

1. **Problem**

A machine fills milk into 500ml packages. It is suspected that the machine is not working correctly and that the amount of milk filled differs from the setpoint  $\mu_0 = 500$ . A sample of 226 packages filled by the machine are collected. The sample mean  $\bar{y}$  is equal to 517.2 and the sample variance  $s_{n-1}^2$  is equal to 262.56.

Test the hypothesis that the amount filled corresponds on average to the setpoint. What is the value of the  $t$  test statistic?

- (a)  $-9.853$
- (b)  $30.505$
- (c)  $-22.761$
- (d)  $-2.894$
- (e)  $15.958$

**Solution**

The  $t$  test statistic is calculated by:

$$t = \frac{\bar{y} - \mu_0}{\sqrt{\frac{s_{n-1}^2}{n}}} = \frac{517.2 - 500}{\sqrt{\frac{262.56}{226}}} = 15.958.$$

The  $t$  test statistic is thus equal to 15.958.

- (a) False
- (b) False
- (c) False
- (d) False
- (e) True