1. Problem

Theory: Consider a linear regression of y on x. It is usually estimated with which estimation technique (three-letter abbreviation)?

This estimator yields the best linear unbiased estimator (BLUE) under the assumptions of the Gauss-Markov theorem. Which of the following properties are required for the errors of the linear regression model under these assumptions?

 $independent \ / \ zero \ expectation \ / \ normally \ distributed \ / \ identically \ distributed \ / \ homoscedastic$

Application: Using the data provided in linreg.csv estimate a linear regression of y on x. What are the estimated parameters?

Intercept:

Slope:

In terms of significance at 5% level:

 \boldsymbol{x} and \boldsymbol{y} are not significantly correlated / \boldsymbol{y} increases significantly with \boldsymbol{x} / \boldsymbol{y} decreases significantly with \boldsymbol{x}

Solution

abline(m)

Theory: Linear regression models are typically estimated by ordinary least squares (OLS). The Gauss-Markov theorem establishes certain optimality properties: Namely, if the errors have expectation zero, constant variance (homoscedastic), no autocorrelation and the regressors are exogenous and not linearly dependent, the OLS estimator is the best linear unbiased estimator (BLUE).

Application: The estimated coefficients along with their significances are reported in the summary of the fitted regression model, showing that y increases significantly with x (at 5% level).

```
Call:
lm(formula = y ~ x, data = d)
Residuals:
                   Median
               1Q
-0.50503 -0.17149 -0.01047 0.13726 0.69840
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.005094 0.023993 -0.212
                                             0.832
             0.558063
                        0.044927 12.421
                                            <2e-16
х
Residual standard error: 0.2399 on 98 degrees of freedom
Multiple R-squared: 0.6116,
                                     Adjusted R-squared: 0.6076
F-statistic: 154.3 on 1 and 98 DF, p-value: < 2.2e-16
Code: The analysis can be replicated in R using the following code.
## data
d <- read.csv("linreg.csv")</pre>
## regression
m < -lm(y \sim x, data = d)
summary(m)
## visualization
plot(y ~ x, data = d)
```